

Course's Name :Calculus II

Palestine Technical University -Kadoorie

Instructor's Name:

Course's Number:



Student's Name:

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firstExam
Second Semester 2016/2017

Form(B)

Question one

(12 points)

Choose the correct answer in the following statements, Then complete the table (use capital letters)

1	2	3	4	5	6	7	8

1) If $y = 3^{\sin x}$, then $\frac{dy}{dx}$ when $x = \pi$ is

- A) 1 B) 0 C) $\ln 3$ D) $-\ln 3$

2) The solution of $\ln x + \ln(x + 1) = 0$ is

- A) $-.1 - \sqrt{2}$ B) $-1 + \sqrt{2}$ C) $-1 \pm \sqrt{2}$ D) $1 + \sqrt{2}$

3) $\sec(\tan^{-1} \frac{x}{2})$

- A) $\frac{\sqrt{x^2 + 4}}{2}$ B) $\sqrt{x^2 + 4}$ C) $\frac{\sqrt{4 + x^2}}{x}$ D) $\frac{x}{\sqrt{4 + x^2}}$

4) If $\cosh x = \frac{5}{4}$, $x < 0$ then $\sinh x =$

- A) $\frac{3}{5}$ B) $\frac{4}{5}$ C) $\frac{-3}{5}$ D) $\frac{-3}{4}$

5) $f(x) = \cosh(\log_2 x)$, then $f'(x) =$

- A) $\frac{\sinh(\log_2 x)}{x \ln 2}$ B) $\sinh(\log_2 x)$ C) $\frac{-\sinh(\log_2 x)}{x \ln 2}$ D) $\frac{\sinh(\log_2 x)}{x}$

6) If f is one-to-one function and $f(5) = 1, f(3) = 5, f'(5) = 3, f'(3) = 4$, then $(f^{-1})'(5) =$

- A) $\frac{1}{3}$ B) 4 C) 3 D) $\frac{1}{4}$

7) If $y = (x)^{\ln x}$ then $\frac{dy}{dx} =$

- A) $\ln x (x)^{(\ln x)-1}$ B) $(\ln x)^{x-1}$ C) $(x)^{\ln x} \left(\frac{2 \ln x}{x}\right)$ D) $(x)^{\ln x} \left(\frac{1}{\ln x} + \ln(\ln x)\right)$

8) $\int_0^1 \frac{1}{\sqrt{4-x^2}} dx$

- A) $\frac{\pi}{6}$ B) $\frac{-\pi}{6}$ C) $\frac{\pi}{3}$ D) $\frac{\pi}{12}$

Question two

(11 points)

- a. Consider the area enclosed between the curve $y = 2x - x^2$ and the x -axis, find the volume of the solid generated by revolving this area about $x = 2$

- b. Find the length of the curve

$$x = \int_0^y \sqrt{(\sec t)^4 - 1} dt, \frac{-\pi}{4} \leq x \leq \frac{\pi}{4}$$

Evaluate the following definite integrals.

a. $\int_1^e \frac{dx}{x[(\ln x)^2 + 1]}$

b. $\int_0^{\ln 2} 2 e^x \sinh x \, dx$

